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# A new model for gas radiative properties applicable to oxy-fuel combustion modelling

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## Introduction

Radiation is the principal mode of heat transfer in furnaces. Modeling of radiation heat transfer in combustion systems is very complicated. There are two key issues, i.e., how to calculate radiation intensity at different locations along different directions from radiative transfer equations and how to evaluate radiation properties at different locations. Different combustion environments (air-fuel or oxy-fuel) make no difference to the 1<sup>st</sup> key issue; they will only affect the gaseous radiative properties.

Models for gaseous radiative properties have been well established for air combustion. However, there is uncertainty regarding their applicability to oxy-fuel conditions. In this paper, a new and complete set of models for gaseous radiative properties is derived, which is applicable to CFD modeling of both air-fuel and oxy-fuel conditions. The derivation, calibration and implementation of the new model are given.

## Method

- First, a computer code is developed to evaluate the emissivity of *any* gas mixture at *any* condition by using the exponential wide band model (EWBM), and the calculated results are calibrated in very details by data in literature.
- Then, the calibrated code is used to generate emissivity databases for representative air-firing and oxy-firing conditions, for each of which a new weighted-sum-of-gray-gases model (WSGGM) with new parameters is derived. The way to implement the new models into CFD simulations of combustion systems is given.
- Finally, as a demonstration, the new models are applied to CFD modeling of a 0.8MW oxy-natural gas flame furnace. The CFD results are compared with those based on the widely used WSGGMs in literature. Based on that, some useful guidelines on oxy-fuel modeling are recommended.

## Result 1: Calibration of EWBM code

Based on “almost exact analytical expressions”, a computer code in c++ is developed to evaluate the emissivity of *any* gas mixture that may consist of H<sub>2</sub>O, CO<sub>2</sub>, CO, CH<sub>4</sub>, NO and SO<sub>2</sub> at *any* condition using the EWBM. The application of this code to a gas mixture is shown below, with almost all the values here calibrated with a reference example.

```
[0] Input Conditions:      Gas temperature, T_g [K] = 1500.00
                          Total pressure, P [Pa] = 101325.00
                          Path length, S [m] = 0.50000
                          Mole fraction: (i=0) x_H2O=0.160; (i=1) x_CO2=0.085; (i=2) x_CO=0.020; (i=3) x_CH4=0.005

***** The detailed calculation results *****
[1] Calculate the lower and upper band limits (n_u, l_u, n_l, l_l) for j-th band of i-th participating species
    n_u [cm]      n_l [cm]      l_u [cm]      l_l [cm]      n_u [1/cm]      n_l [1/cm]
H2O (i=0)
  71.43 (i=0) 11.7090 1.2753 268.398 4327.750522 0.03895 879.403 0.3052 1265.701 0.000 772.850
  6.45 (i=1) 11.7090 1.2753 116.426 41.10000 0.27712 259.232 0.0552 640.322 1279.379 1920.161
  2.66 (i=2) 11.7090 1.2753 232.379 24.95037 0.40010 253.996 0.7334 952.754 3283.623 4236.377
  1.87 (i=3) 11.7090 1.2753 166.926 3.81281 0.27365 45.146 0.9000 451.465 5123.272 5576.728
  1.38 (i=4) 11.7090 1.2753 123.935 2.64763 0.20987 31.001 0.9000 310.011 7094.995 7405.005
CO (i=1)
  14.39 (i=0) 15.1962 1.0178 49.187 19.00000 1.12948 136.241 0.3610 213.219 560.391 773.609
  10.42 (i=1) 15.1962 1.0203 51.898 0.15031 0.30051 2.176 0.9000 2.756 948.122 971.878
  9.43 (i=2) 15.1962 1.0203 39.117 0.158436 2.66500 2.408 0.9000 24.076 1047.962 1072.038
  773.609 948.122 971.878 110.00000 0.95962 201.774 0.2110 25.000 2132.970 2110.000
  2.73 (i=3) 15.1962 1.0203 43.377 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000 0.00000
  1.87 (i=4) 15.1962 1.0165 91.015 5.93672 1.30914 90.473 0.9000 904.730 3207.635 4212.365
  1.38 (i=5) 15.1962 1.0165 133.618 0.138024 12.02135 2.097 0.9000 20.974 5189.513 5210.487
CO2 (i=0)
  4.67 (i=0) 2.2757 1.0016 98.761 20.90000 0.05205 26.148 0.5984 65.118 2110.441 2175.559
  2.35 (i=1) 2.2757 1.0000 77.460 0.13722 0.412 0.9000 0.412 0.9000 4257.939 4262.061
OH (i=1)
  7.53 (i=0) 0.3259 1.0012 81.333 28.00000 2.03872 9.124 0.9000 91.238 1264.381 1355.619
  3.11 (i=1) 0.3259 1.0012 216.887 46.00000 1.53867 14.989 0.9000 149.892 2945.054 3094.946
  2.37 (i=2) 0.3259 1.0012 232.379 4.48850 0.90280 1.384 0.9000 0.90280 1.384 0.9000 4213.078 4216.922
  1.71 (i=3) 0.3259 1.0012 174.284 0.811220 23.42482 0.264 0.9000 2.644 5859.678 5862.322
[2] Calculate band transmittances (tau_1, tau_2, tau_3), Planck blackbody fractional function (F_u, F_l), and total emissivity
    n_u [cm]      n_l [cm]      l_u [cm]      l_l [cm]      F_u      F_l      tau_1      tau_2      tau_3      emissivity
560.391 772.850 0.000 0.3052 1.0000 0.3652 1.00000 0.00000 0.98352 0.00450
560.391 772.850 0.000 0.3052 1.0000 0.3652 1.00000 0.00000 0.98352 0.00450
772.850 971.878 0.000 0.3610 1.0000 0.3610 1.00000 0.00000 0.98433 0.00007
773.609 948.122 0.000 0.3610 1.0000 0.3610 1.00000 0.00000 0.98433 0.00007
948.122 971.878 0.000 0.9000 1.0000 0.9000 0.97258 0.97116 0.000181 0.00000
971.878 1047.962 0.000 0.9000 1.0000 0.9000 0.97116 0.96451 0.00001 0.00000
1047.962 1072.038 0.000 0.9000 1.0000 0.9000 0.96451 0.96280 0.000012 0.00000
1072.038 1100.000 0.000 0.9000 1.0000 0.9000 0.96280 0.96046 0.000004 0.00000
1264.381 1279.839 0.000 0.9000 1.0000 0.9000 0.94346 0.94172 0.0000174 0.00000
1279.839 1355.619 0.000 0.9000 1.0000 0.9000 0.94172 0.93842 0.0000132 0.00000
1355.619 1920.161 0.000 0.9000 1.0000 0.9000 0.93842 0.93622 0.0000147 0.00000
1920.161 2110.441 0.000 0.9000 1.0000 0.9000 0.93622 0.93445 0.000015 0.00000
2110.441 2175.559 0.000 0.9000 1.0000 0.9000 0.93445 0.93267 0.000015 0.00000
2175.559 2410.000 0.000 0.9000 1.0000 0.9000 0.93267 0.93089 0.000015 0.00000
2410.000 2945.054 0.000 0.9000 1.0000 0.9000 0.93089 0.92911 0.000015 0.00000
2945.054 3094.946 0.000 0.9000 1.0000 0.9000 0.92911 0.92733 0.000015 0.00000
3094.946 3207.635 0.000 0.9000 1.0000 0.9000 0.92733 0.92555 0.000015 0.00000
3207.635 3283.623 0.000 0.9000 1.0000 0.9000 0.92555 0.92377 0.000015 0.00000
3283.623 4212.365 0.000 0.9000 1.0000 0.9000 0.92377 0.92199 0.000015 0.00000
4212.365 4213.078 0.000 0.9000 1.0000 0.9000 0.92199 0.92021 0.000015 0.00000
4213.078 4236.377 0.000 0.9000 1.0000 0.9000 0.92021 0.91843 0.000015 0.00000
4236.377 4257.939 0.000 0.9000 1.0000 0.9000 0.91843 0.91665 0.000015 0.00000
4257.939 4262.061 0.000 0.9000 1.0000 0.9000 0.91665 0.91487 0.000015 0.00000
4262.061 5123.272 0.000 0.9000 1.0000 0.9000 0.91487 0.91309 0.000015 0.00000
5123.272 5189.513 0.000 0.9000 1.0000 0.9000 0.91309 0.91131 0.000015 0.00000
5189.513 5210.487 0.000 0.9000 1.0000 0.9000 0.91131 0.90953 0.000015 0.00000
5210.487 5576.728 0.000 0.9000 1.0000 0.9000 0.90953 0.90775 0.000015 0.00000
5576.728 5859.678 0.000 0.9000 1.0000 0.9000 0.90775 0.90597 0.000015 0.00000
5859.678 5862.322 0.000 0.9000 1.0000 0.9000 0.90597 0.90419 0.000015 0.00000
5862.322 7094.995 0.000 0.9000 1.0000 0.9000 0.90419 0.90241 0.000015 0.00000
7094.995 7405.005 0.000 0.9000 1.0000 0.9000 0.90241 0.90063 0.000015 0.00000
7405.005 10000.00 0.000 0.9000 1.0000 0.9000 0.90063 0.90000 0.000015 0.00000
( -, - ) means "no band"
sum = 0.167256724
The total emissivity of the mixture at the above condition, epsilon = 0.167256724
The equivalent (gray) absorption coefficient, -(1/S)*log(1-epsilon) = 0.368059752
```

The detailed results of the EWBM code applied to calculate the total emissivity of an arbitrary gas mixture.

## Result 2: The new models

The complete set of the new models consists of the following equations and new parameters for a number of representative air-fuel and oxy-fuel conditions, and the way to implement them into CFD modeling. Here, only the new WSGGM parameters for the representative oxy-fuel conditions are listed, as seen in Table 1.

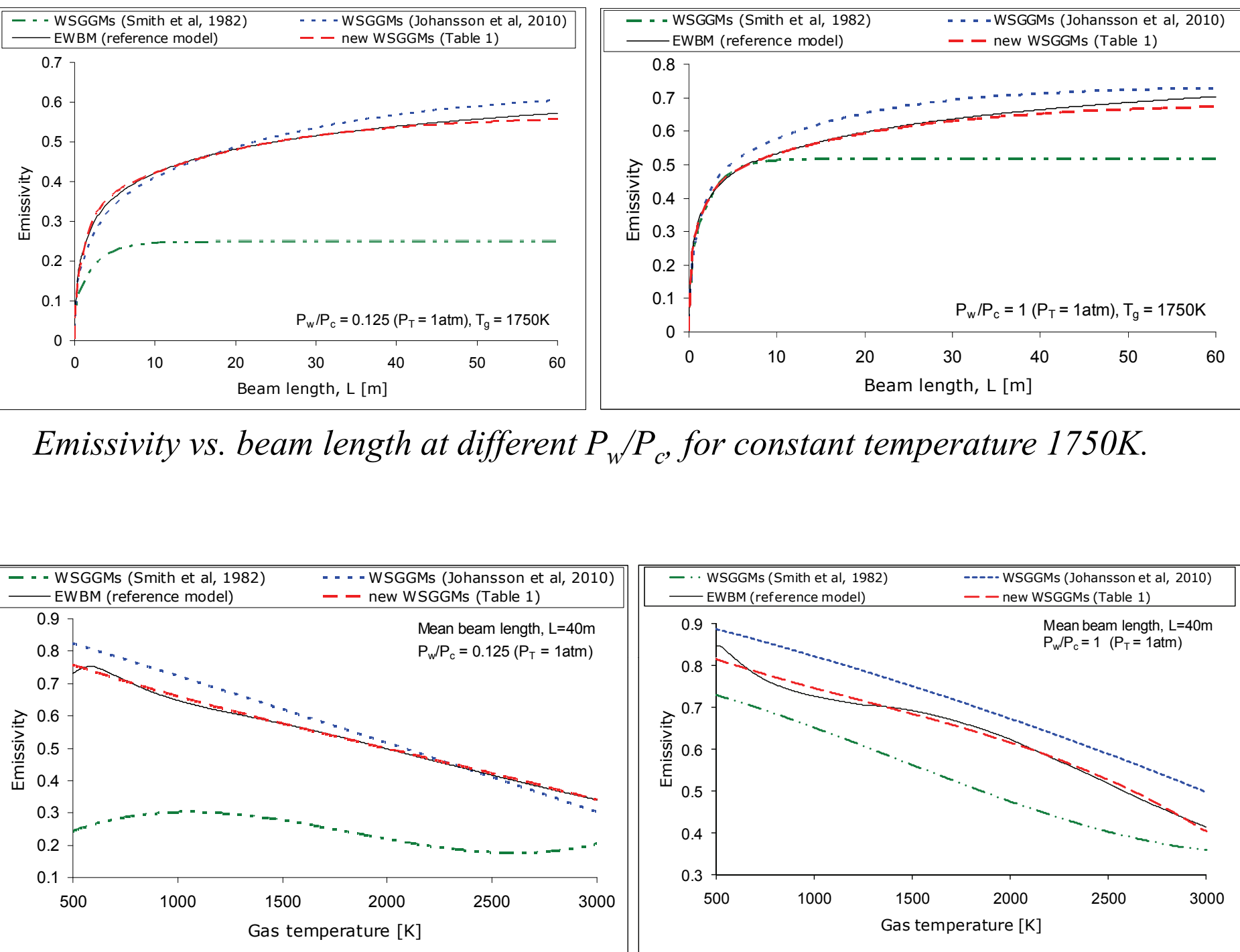
$$\varepsilon = \sum_{i=0}^I a_{\varepsilon,i}(T_g) \cdot \left(1 - e^{-k_i \cdot P \cdot L}\right)$$

$$\left\{ \begin{array}{l} a_{\varepsilon,i}(T) = \sum_{j=1}^J b_{\varepsilon,i,j} \left( \frac{T_g}{T_{\text{ref}}} \right)^{j-1} \quad i=1, \dots, I \quad a_{\varepsilon,i} > 0 \\ I = 4, \quad J = 4, \quad T_{\text{ref}} = 1200 \text{ (in the unit of K) for a better estimate} \\ k_0 = 0: \text{represent 'windows' in the spectrum; } a_{\varepsilon,0} = 1 - \sum_{i=1}^I a_{\varepsilon,i} > 0 \\ P: \text{the sum of the partial pressures of all the participating gases, atm} \end{array} \right.$$

Table 1. New parameters for the WSGGMs, applicable to oxy-fuel flames.

i	k <sub>i</sub>	b <sub>ε,i,1</sub>	b <sub>ε,i,2</sub>	b <sub>ε,i,3</sub>	b <sub>ε,i,4</sub>
P <sub>w</sub> → 0 atm, P <sub>c</sub> → 0 atm					
1	0.009422	0.778969	-1.342848	0.964858	-0.155747
2	0.015546	-0.011449	0.343754	-0.234886	0.044008
3	11.617018	-0.007027	0.242233	-0.173738	0.033868
4	319.911168	0.080082	-0.049280	0.001861	0.002232
P <sub>w</sub> = 0.1 atm, P <sub>c</sub> = 0.1 atm					
1	0.256738	0.492304	-0.483789	0.279329	-0.057770
2	0.080233	0.082666	-0.360752	0.070509	0.044008
3	52.585782	0.114385	-0.083662	0.002003	0.003902
4	440.845718	0.079515	-0.110361	0.051379	-0.007983
P <sub>w</sub> = 0.3 atm, P <sub>c</sub> = 0.1 atm					
1	0.132242	0.478371	-0.698643	0.470598	-0.109044
2	14.660767	0.101065	0.204118	-0.202202	0.042771
3	1.750654	0.185155	0.299794	-0.240346	0.046968
4	165.763926	0.191665	-0.277448	0.135514	-0.021280
P <sub>w</sub> /P <sub>c</sub> = 1/8, P <sub>w</sub> + P <sub>c</sub> = 1 atm (corresponding to dry flue gas recycling, FGR)					
1	0.051237	0.515415	-0.618162	0.430921	-0.092082
2	0.688383	0.199807	0.298581	-0.265758	0.052910
3	13.763205	0.138767	-0.001851	-0.049353	0.013012
4	289.841885	0.087511	-0.067295	0.013489	-5.54E-06
P <sub>w</sub> /P <sub>c</sub> = 1/4, P <sub>w</sub> + P <sub>c</sub> = 1 atm					
1	0.052594	0.486247	-0.644137	0.485654	-0.107808
2	0.752776	0.213959	0.306543	-0.264417	0.051889
3	11.543306	0.181991	-0.020460	-0.053791	0.015058
4	252.93841	0.106180	-0.096088	0.028114	-0.002443
P <sub>w</sub> /P <sub>c</sub> = 1/2, P <sub>w</sub> + P <sub>c</sub> = 1 atm					
1	0.052378	0.383225	-0.510637	0.442201	-0.106398
2	0.712283	0.251481	0.161562	-0.150405	0.028982
3	8.067637	0.208239	0.070697	-0.135668	0.032090
4	195.892573	0.147259	-0.156339	0.057698	-0.007266
P <sub>w</sub> /P <sub>c</sub> = 3/4, P <sub>w</sub> + P <sub>c</sub> = 1 atm					
1	0.051639	0.255953	-0.276222	0.311285	-0.084903
2	0.617739	0.340392	-0.126902	0.051357	-0.010259
3	6.051770	0.160253	0.289548	-0.284144	0.000344
4	150.875915	0.201452	-0.233937	0.095159	-0.013302
P <sub>w</sub> /P <sub>c</sub> = 1/1, P <sub>w</sub> + P <sub>c</sub> = 1 atm (corresponding to wet FGR)					
1	0.051487	0.164048	-0.087793	0.195253	-0.063573
2	0.571797	0.412652	-0.339810	0.197886	-0.038963
3	5.398936	0.112364	0.450929	-0.388486	0.079862
4	130.622859	0.238339	-0.288619	0.121962	-0.017651
P <sub>w</sub> /P <sub>c</sub> = 2/1, P <sub>w</sub> + P <sub>c</sub> = 1 atm (corresponding to, e.g., oxy-fuel combustion of natural gas, without FGR)					
1	0.054480	-0.002188	0.286129	-0.048594	-0.016243
2	0.555304	0.546857	-0.714799	0.452812	-0.088841
3	5.040174	-0.001911	0.764177	-0.581819	0.115069
4	100.272663	0.317219	-0.415470	0.186570	-0.028335
P <sub>w</sub> /P <sub>c</sub> = 4/1, P <sub>w</sub> + P <sub>c</sub> = 1 atm					
1	0.060800	-0.053959	0.434975	-0.152413	0.005094
2	5.608831	-0.094953	0.952010	-0.696161	0.136316
3	0.676040	0.606525	-0.853216	0.545562	-0.107328
4	84.540632	0.369661	-0.517493	0.244011	-0.038451

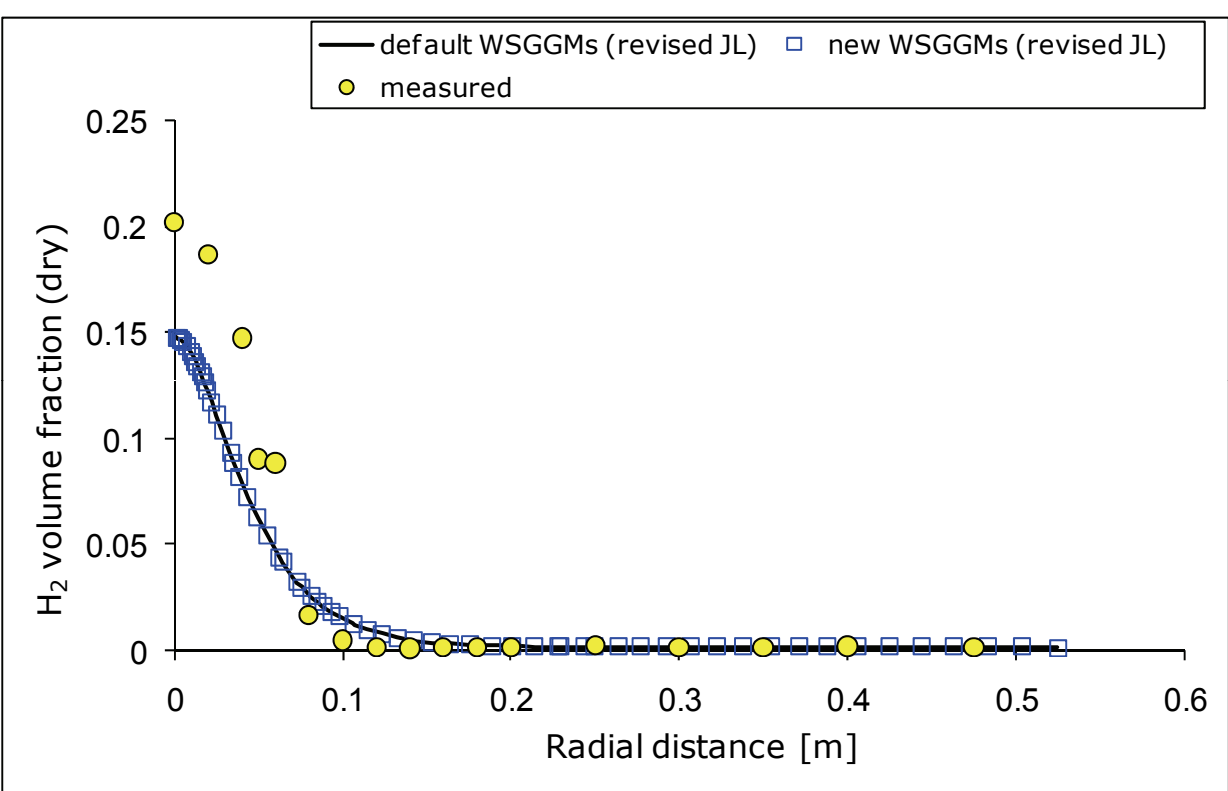
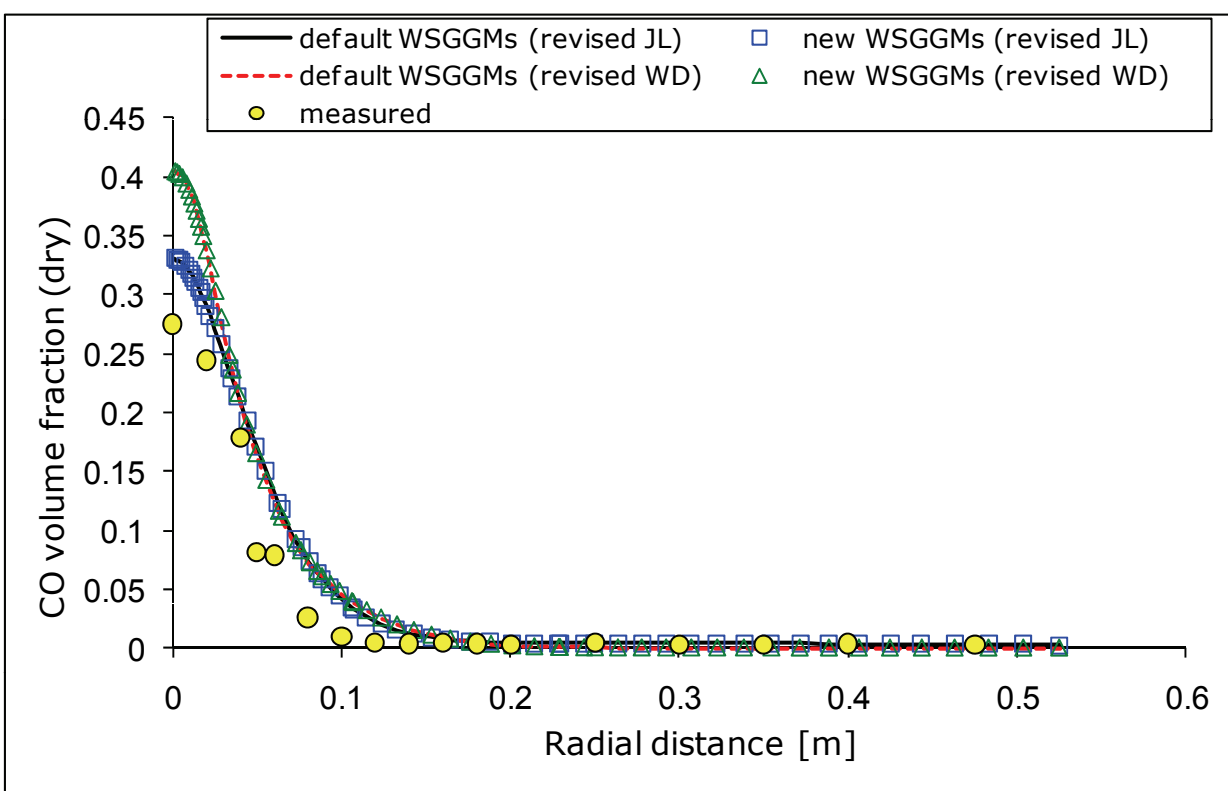
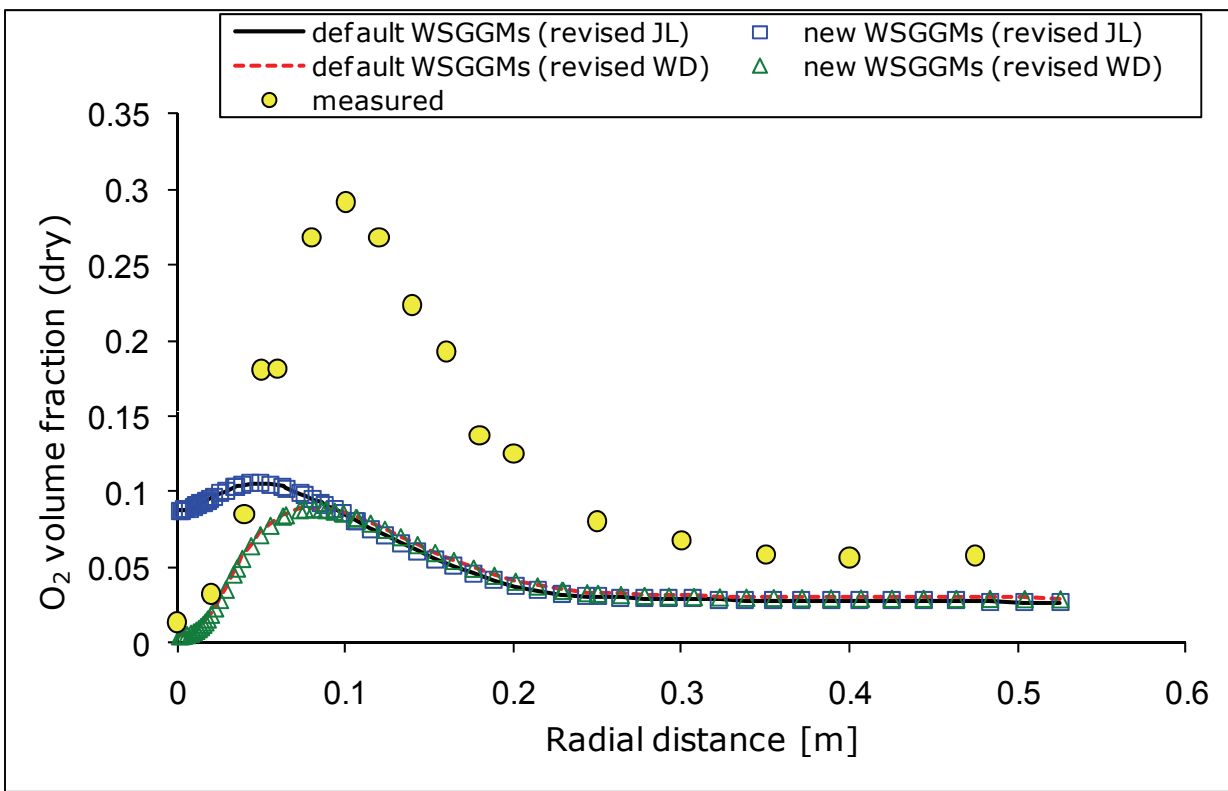
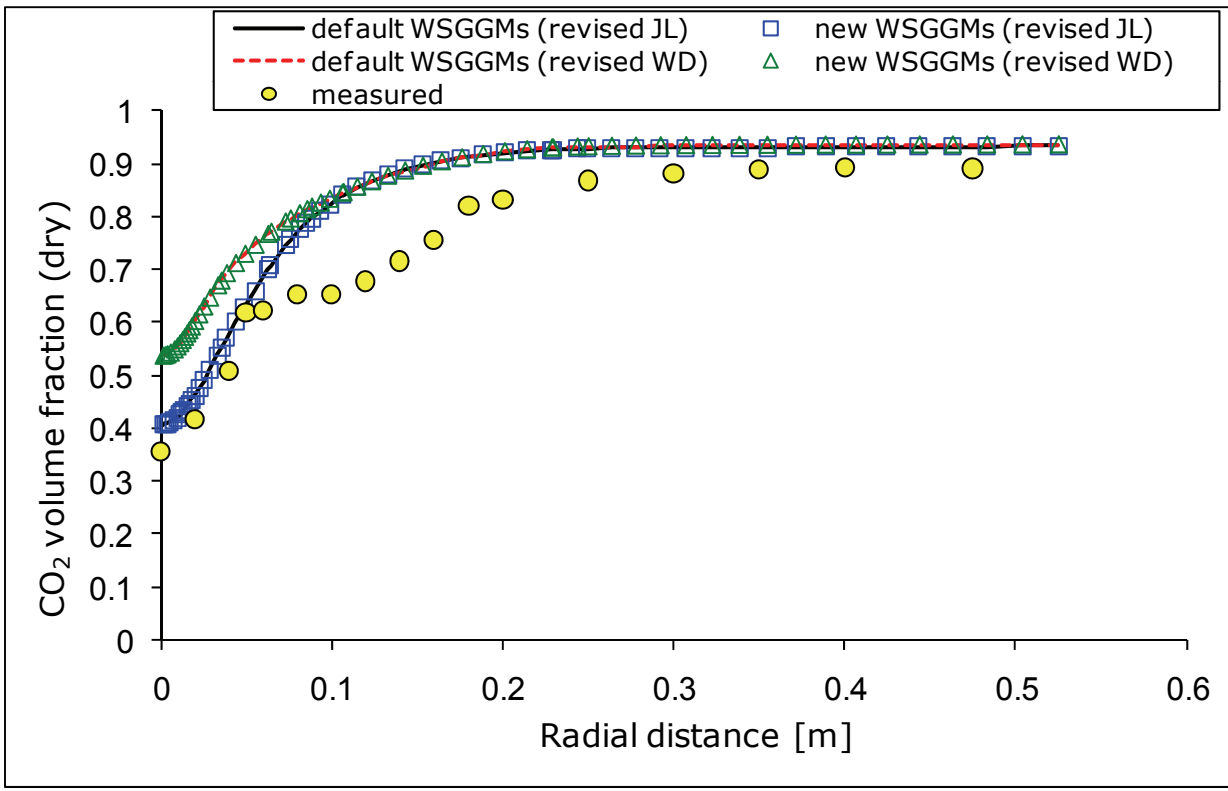
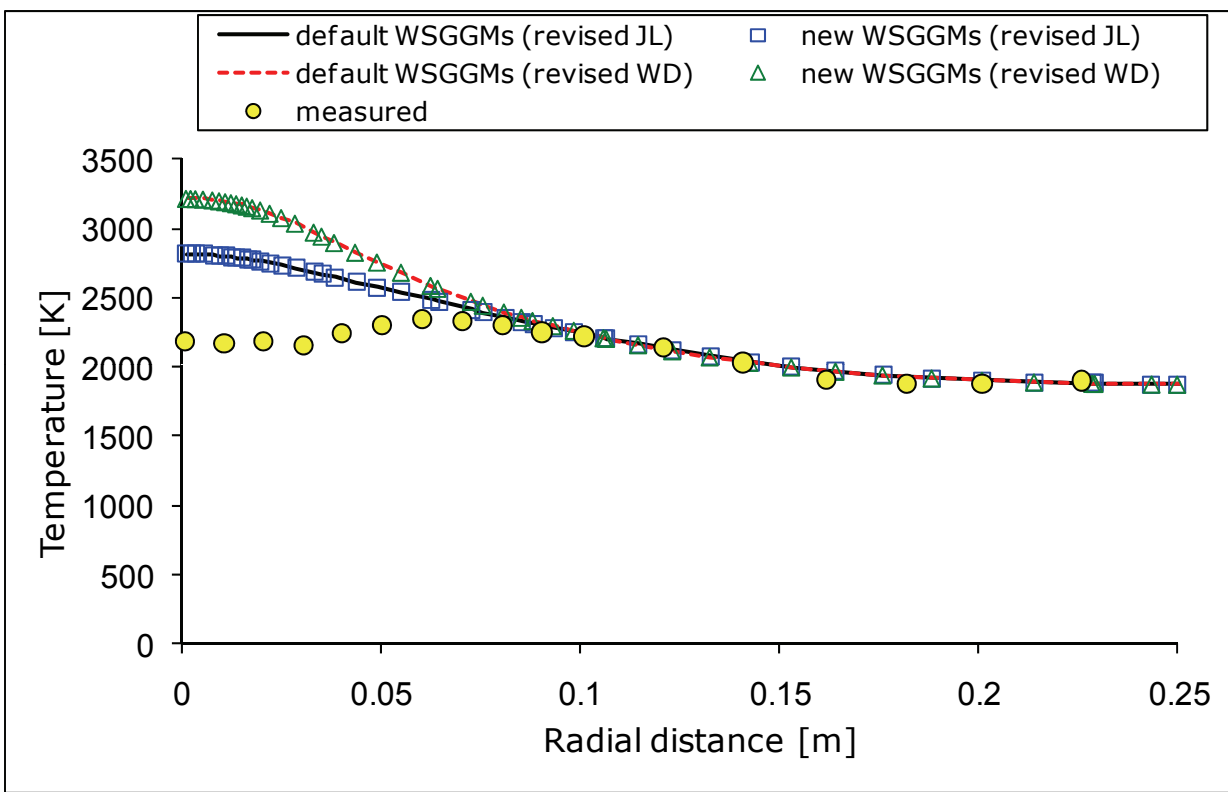
P<sub>w</sub>, P<sub>c</sub> and P<sub>w</sub>/P<sub>c</sub> are never constant throughout any real combustion system. The parameters of different representative conditions will be used based on local gas conditions in the combustion system under modeling.



Emissivity vs. gas temperature at different P<sub>w</sub>/P<sub>c</sub> for constant beam length 40m.

## Result 3: Demonstration

The new models have been applied to CFD of a 0.8MW IFRF oxy-natural gas flame furnace.



## Conclusions

The new WSGGMs need to be used in CFD modeling of large-scale oxy-fuel furnaces. For small-scale facilities, they do not make remarkable difference. Combustion chemistry also plays a key role in oxy-firing modelling.

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